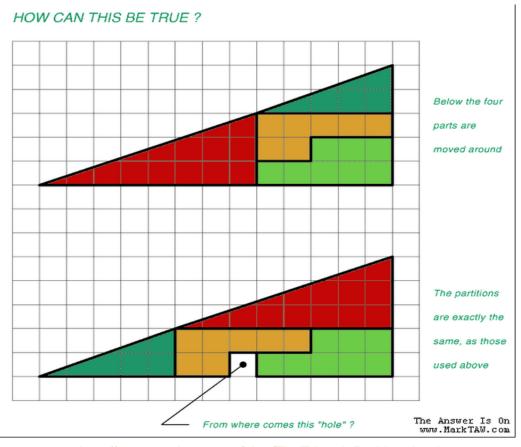
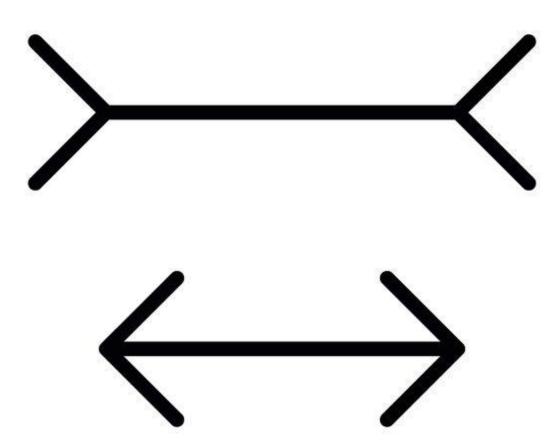
TIM KRASKA

LYING WITH STATISTICS AND VISUALIZATIONS



http://www.marktaw.com/blog/TheTriangleProblem.html

SURVEYS



LYING WITH NUMBERS

"The average market salary for MIT graduates with 0-2 years of experience is \$151,000 per year"

In how many ways can this be misleading?

SAMPLING BIAS

- More successful graduates are more likely to respond to surveys
 - They feel good about their earnings
 - Surveys are only sent to big companies
- How big is their sample size?
 - Not disclosed
- Tendency to exaggerate
 - Brag about your salary
 - School spirit, want your alma mater to rank highly
- Tendency to minimize
 - No one likes tax
- Do they cancel out each other?
 - No one knows!

LYING WITH NUMBERS

"The average market salary for MIT graduates with 0-2 years of experience is \$151,000 per year"

In how many ways can this be misleading?

THE TERM "AVERAGE"

- Imagine a school with 5 alumni
 - o Bill Doors: \$1 million/year
 - Mark Bergkerzuck: \$120k/year
 - Larry Sheet: \$100k/year
 - Sergey Bin: \$80k/year
 - Steve Baller: \$80k/year
- Average can be mean, median, or mode; They can be totally different
- Mean: Evenly distributes the total among individuals
 - Can be unrepresentative when measurements are highly skewed
 - In our example: \$276k/year
- Median: Value dividing distribution into two equal parts (50th percentile)
 - In our example: \$100k/year
- Mode: Most frequently observed outcome (rarely reported with numeric data)
 - In our example: \$80k/year

FINAL SENTENCE

"The average market salary for MIT graduates with 0-2 years of experience is \$151,000 per year"

PayScale's methodology did not include alums with advanced degrees and only used data from graduates with bachelor's degrees. It also excluded self-employed and contract employees.

Because the salaries of graduates from elite schools vary extensively, the study has a relatively wide margin of error, the report stated.

CORRELATION VS CAUSATION

What conclusions can you make from this data?

Does going to MIT make you rich?

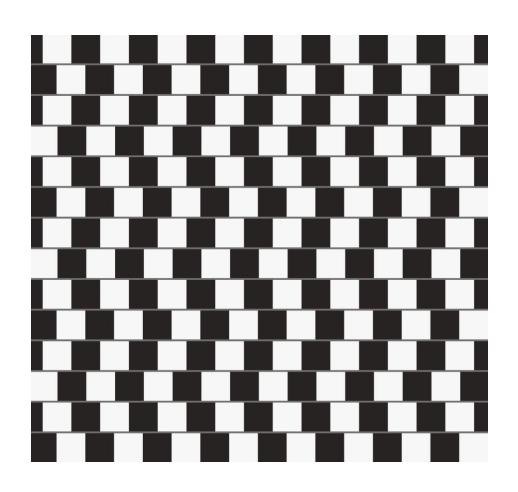


LYING WITH SURVEYS

Three questions you should ask after you read any paper:

- 1. Is there any bias in the sample set?
 - a. Look for unconscious bias
 - b. Look for conscious bias
- 2. What statistics are they actually talking about?
- 3. What conclusions can we make from their findings?

LYING WITH VISUALIZATIONS

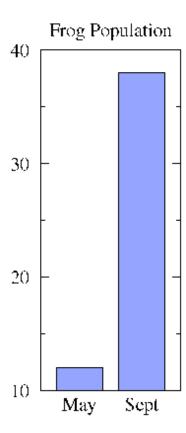


LYING WITH VISUALIZATION

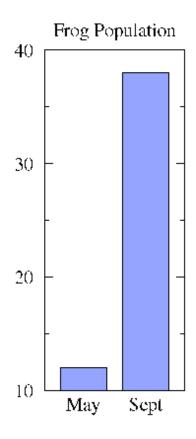
seeing is believing

"don't believe everything you see."

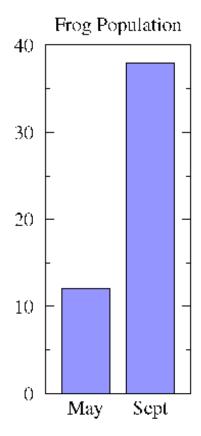
LYING WITH BAR CHARTS



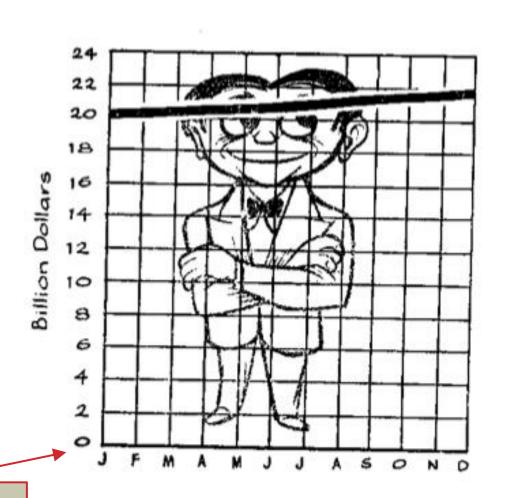
LYING WITH BAR CHARTS



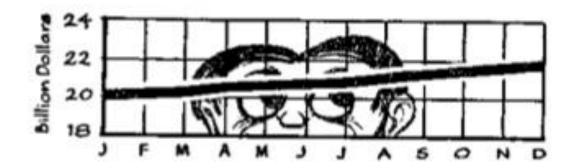




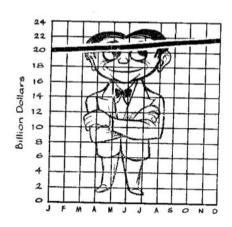
LYING WITH LINE CHART

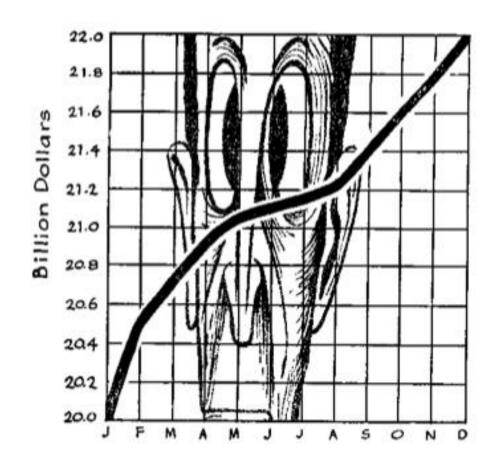


CHOP OFF THE BOTTOM



CHANGE THE PORTION OF Y-AXIS

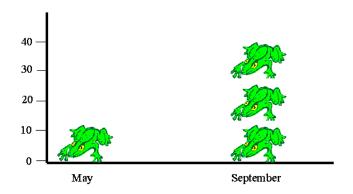




LYING WITH DIAGRAM

- Say that in a pond, there were
 - 13 Adult frogs in May
 - o 39 Adult frogs in September
- Represented in a "stacked-frog" plot

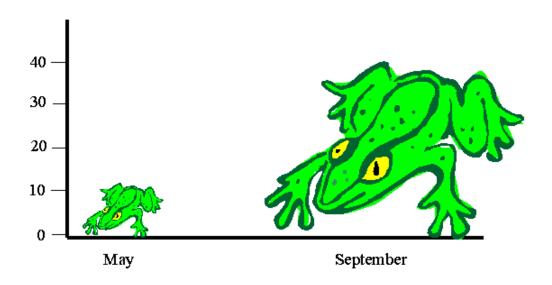
Number of Adult Frogs in South Pond



LYING WITH DIAGRAM

or we can represent in this way...

Number of Adult Frogs in South Pond



http://www.physics.csbsju.edu/stats/display.html

SOME MORE EXAMPLE

People at "A" get twice pay than people at "B"





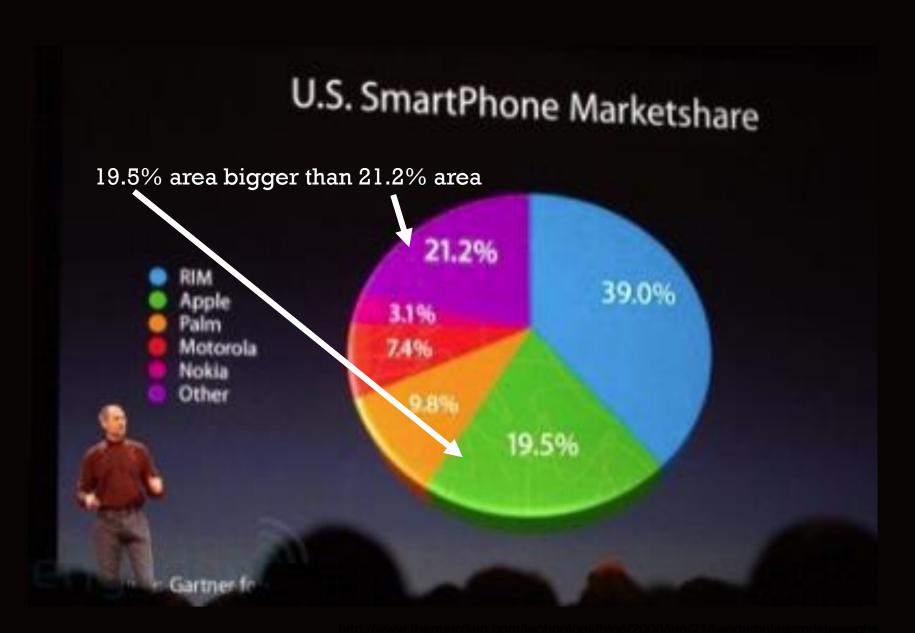
LYING WITH 3D



APPLE WWDC 2008

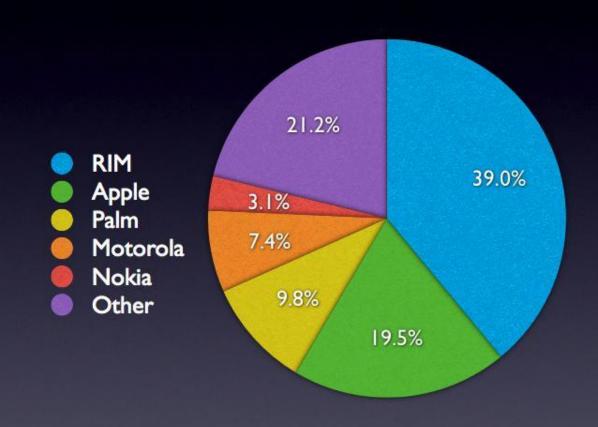


APPLE WWDC 2008



TODAY'S EXAMPLE (APPLE WWDC 2008)

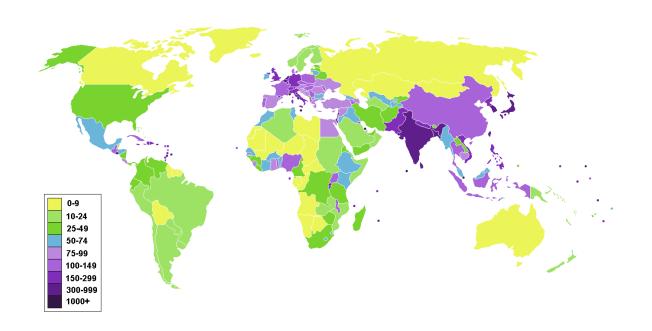
U.S. SmartPhone Marketshare



LYING WITH MAPS

Choropleth map

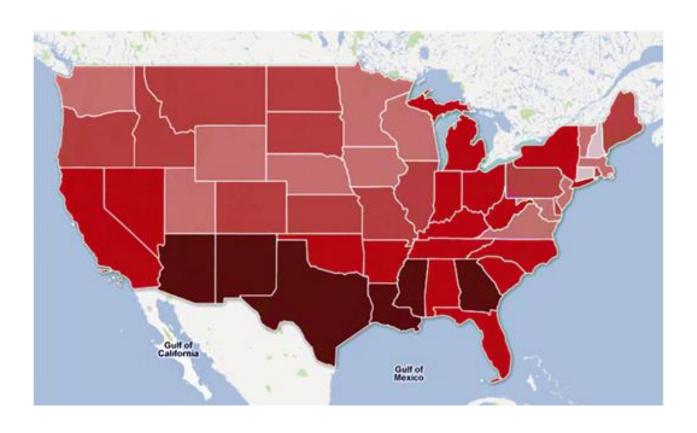
 provides an easy way to visualize measurement varies across geographic area



http://upload.wikimedia.org/wikipedia/commons/1/17/World_population_density_map.png

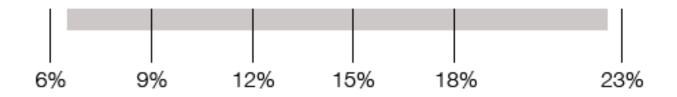
LYING WITH CHOROPLETH MAP

US poverty map from Guardian data blog

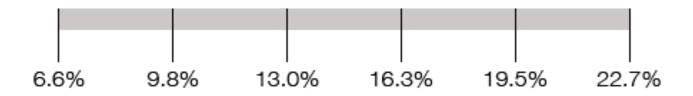


LYING WITH CHOROPLETH MAP

- Poverty data range from 6.6% to 22.7%
 - Unequally distributed

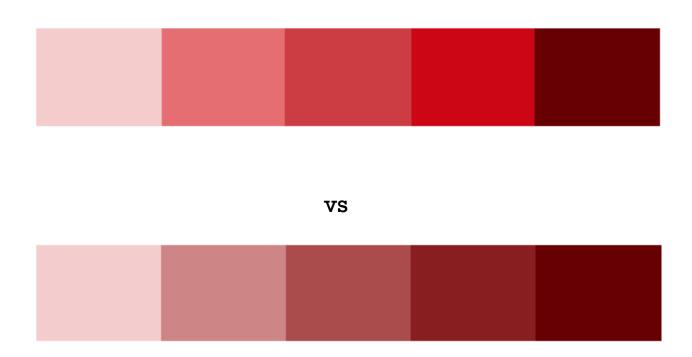


If we are measuring inequality, perhaps we should at least use equally distributed classes



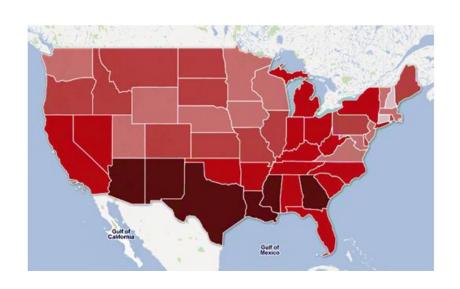
CHOICE OF COLOR

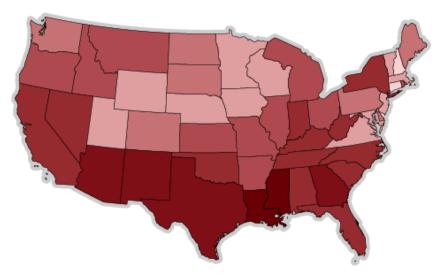




LYING WITH CHOROPLETH MAP

With equally distributed classes and equidistant colors from a HSV gradient

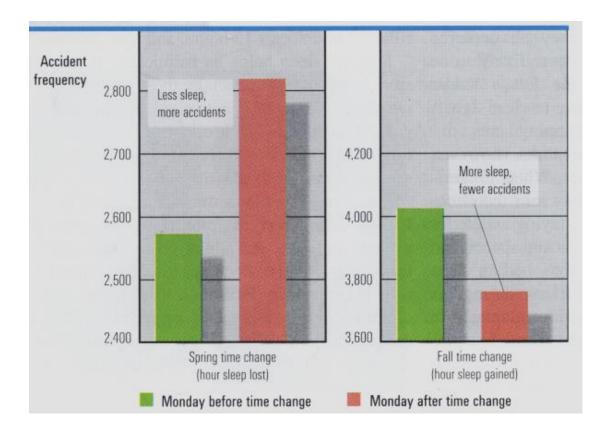




LYING WITH CHOROPLETH MAP

- When look at any choropleth map, be aware of
 - How they categorize the classes
 - How they choose the colors
- Choropleth map classification based on
 - Equal-intervals
 - quantile classing; each class has equal number quantity
 - lterative algorithm to find "natural breaks"

CLASS QUESTION



The above graphic was copied from a book about sleep research. The bars try to summarize the number of traffic accidents in Canada before and after daylight-savings time adjustments for the years 1991 and 1992 (combined). The goal of the graph is to suggest a correlation between lost sleep and traffic accidents.

LYING THROUGH AGGREGATIONS

	Smoker?			
	Yes	No		
Dead	107	132		
Alive	174	175		
Total	281	307		
% Dying	38.1%	43.0%		

(data adapted from Appleton et al. 1996, Am. Stat.)

MOTIVATING EXAMPLE: SMOKING & SURVIVAL

20-year follow-up study, Wickham in UK (Tunbridge et al. 1977)

1972-1974, one-in-six survey of the electoral roll, largely concerned with thyroid disease and heart disease

For simplicity, consider women aged 45 to 75 at the start of the study

- Smoking status: current smoker (Y/N)
- 20-year survival info: determined for all women in the study

	Smoker?			
	Yes	No		
Dead	107	132		
Alive	174	175		
Total	281	307		
% Dying	38.1%	43.0%		

Protective effect of smoking?

SMOKING & SURVIVAL (CON'T)

	Age Group						
	45-54		55-64		65-74		
	Smoker?		Smoker?		Smoker?		
	Yes	No	Yes	No	Yes	No	
Dead	27	12	51	40	29	101	
Alive	103	66	64	81	7	28	
Total	130	78	105	121	36	129	
% Dying	20.8%	15.4%	48.6%	33.1%	80.6%	78.3%	

Consider 10-year ranges: 45-54,55-64,65-75

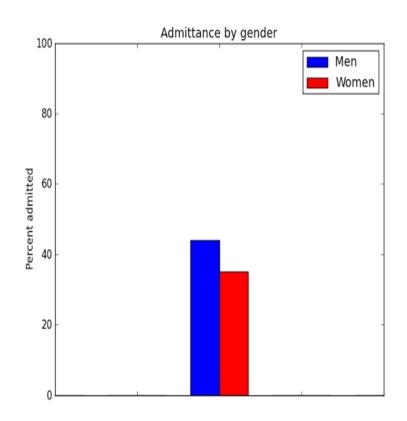
Non-smoking group does better in each case!

GENDER BIAS, OR NOT?

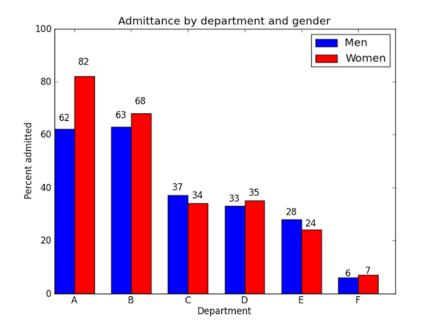
1973, UC Berkeley was afraid to be sued for discrimination against women in graduate school admissions

Percent acceptance: Male vs Female,

44% vs. 35%



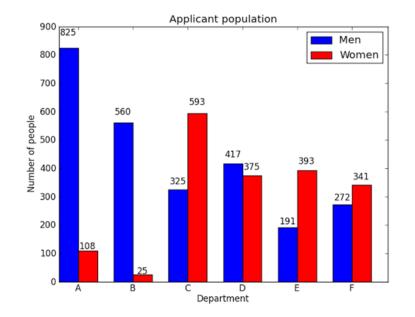
GENDER BIAS, OR NOT? (CONT'D)



P. J. Bickel, E. A. Hammel, J. W. O'Connell. (1975). Sex Bias in Graduate Admissions: Data from Berkeley. Science 187, (4175). pp. 398-404

Table 2. Admissions data by sex of applicant for two hypothetical departments. For total, $\chi^2 = 5.71$, d.f. = 1, P = 0.19 (one-tailed).

Applicants	Outcome			Difference		
	Observed		Expected		Difference	
	Admit	Deny	Admit	Deny	Admit	Deny
		Departm	ent of machis	matics		
Men	200	200	200	200	0	0
Women	100	100	100	100	0	0
	105.500	Departme	ent of social w	varfare		
Men	50	100	50	100	0	0
Women	150	300	150	300	0	0
***************************************			Totals			
Men	250	300	229.2	320.8	20.8	-20.8
Women	250	400	270.8	379.2	-20.8	20.8



SIMPSON PARADOX

If we have

$$\frac{a}{b} < \frac{A}{B}$$
 and $\frac{c}{d} < \frac{C}{D}$,

is it also true that

$$\frac{a+c}{b+d} < \frac{A+C}{B+D}$$
?

Not necessarily! Note that

$$\frac{1}{3} < \frac{3}{8}$$
 and $\frac{5}{8} < \frac{2}{3}$

but

$$\frac{1+5}{3+8} > \frac{3+2}{8+3}$$

Be aware of the dangers of ignoring a covariate that is correlated to an outcome variable and an explanatory one.

Simpson, E.H. (1951). "The interpretation of Interaction in Contingency Tables", *Journal of the Royal Statistical Society*, B, 13, 238-241.

MORE RECENT EXAMPLE

TechCrunch

Google found it paid men less than women for the same job

by Megan Rose Dickey https://techcrunch.com/2019/03/04/google-found-it-paid-men-less-than-women-for-the-same-job/

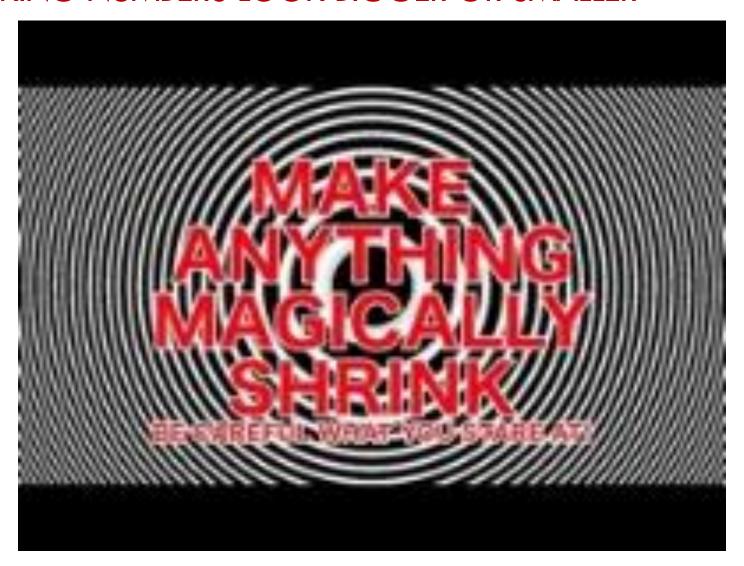
Wired

Are men at Google Paid less than women? Not Really [SEP]

by Natasha Tiku https://www.wired.com/story/men-google-paid-less-than-women-not-really/

IMPRESSIVE FIGURES

MAKING NUMBERS LOOK BIGGER OR SMALLER



MAKING NUMBERS LOOK BIGGER

"runs up to 10x faster"

(https://www.digitalengineering247.com/article/altair-optistructruns-up-to-10x-faster-on-nvidia-gpus)

"lasts up to 5x longer"

(https://ca.crest.com/en-ca/products/crest-complete-whitening-plus-scope-outlast-toothpaste)

"cleans up to 10x better"

(https://www.youtube.com/watch?v=Yx9iCKKzYR4)

UP-TOS

"runs up to 10x faster" [SEP]

(https://www.digitalengineering247.com/article/altair-optistructruns-up-to-10x-faster-on-nvidia-gpus)

"lasts up to 5x longer"

(https://ca.crest.com/en-ca/products/crest-complete-whitening-plus-scope-outlast-toothpaste)

"cleans up to 10x better"

(https://www.youtube.com/watch?v=Yx9iCKKzYR4)

"Schism consistently outperforms simple partitioning schemes, ..., reducing the cost of distributed transactions **up to 30**%"

Carlo Curino, Yang Zhang, Evan P. C. Jones, Samuel Madden: Schism: a Workload-Driven Approach to Database Replication and Partitioning. PVLDB 3(1): 48-57 (2010)

Example (from Colton)

Sex and race distribution of 158 cases of abdominal aortic aneurysms (AAA) at metropolitan hospitals in a Southern city

Sex & Race	#AAA
White Males	93
AA Males	30
White Females	22
AA Females	13

Author's conclusion: Incidence of AAA is almost 3 times more frequent in Whites than African-Americans.

Clicker: Do you see a potential problem?

Example (from Colton)

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Sex & Race	#AAA
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AA Females	13

Author's conclusion: Incidence of AAA is almost 3 times more frequent in Whites than African-Americans.

Do you see a potential problem?

This fallacy is known as a lack of denominators

EXCEPTION FALLACY

HTTPS://CLICKER.MIT.EDU/6.S079/

4 out of 6 members of the math team representing Canada at the 2018 International Math Olympiad were from Ontario.

Clicker: Does Ontario have the best K-12 math curriculum in Canada?

- a) Yes
- b) No
- c) Impossible to say
- d) Scooby-doo

EXCEPTION FALLACY

4 out of 6 members of the math team representing Canada at the 2018 International Math Olympiad were from Ontario.

Does Ontario have the best K-12 math curriculum in Canada?

Note that Ontario has 40% of the nation's population.

DO YOU SEE A PROBLEM WITH THIS LIST?

Example: The Top 10 All Time Grossing Films (in Millions – US)

- 1) Avatar (2009): \$760
- 2) Titanic(1997): \$658
- 3) Marvel's the Avengers (2012): \$588
- 4) The Dark Knight (2008): \$533
- 5) Star Wars I: The Phantom Menace (1999) \$474
- 6) Star Wars IV: A New Hope (1977): \$460
- 7) The Dark Knight Rises (2012) \$449
- 8) Shrek 2 (2011): \$441
- 9) E.T. The Extra-Terrestrial (1982): \$435
- 10) The Hunger Games: Catching Fire (2013): \$424



REAL VS. NOMINAL VARIABLES



Nominal Variables are in terms of a current dollars. For example, you're starting salary after college might be \$50,000 per year.

Real variables are in terms of some fixed commodity. Real variables measure purchasing power. If a gallon of gas costs \$2.00, then we can calculate your "real" income.

Real Income =
$$\frac{\text{Nominal Income}}{\text{Price}} = \frac{\$50,000}{\$2.00} = 25,000$$





In 2009, a gallon of gas cost \$3.50

Real Gross =
$$\frac{\text{Nominal Gross}}{\text{Price}} = \frac{\$749\text{M}}{\$3.50} = 214\text{M}$$
(Gallons of Gas)



In 1977, a gallon of gas cost \$.62

Real Income =
$$\frac{\text{Nominal Gross}}{\text{Price}} = \frac{\$460\text{M}}{\$.62} = 742\text{M}$$
(Gallons of Gas)

The Top 10 All Time Grossing Films— Inflation Adjusted (Millions of 2000 Dollars)

- 1) Gone With the Wind (1939): \$1,689
- 2) Star Wars Episode IV(1977): \$960
- 3) The Sound of Music(1965): \$768
- 4) ET: The Extraterrestrial(1982): \$764
- 5) The Ten Commandments (1956): \$706
- 6) Titanic (1997): \$691
- 7) Jaws (1975): \$690
- 8) Dr. Zhivago (1965): \$669
- 9) The Exorcist (1973): \$596
- 10) Snow White (1937): \$587



Notes: Avatar falls to #14 (\$516), a movie ticket in 1939 was \$0.23

SELF-DRIVING CARS

[Tesla] said Autopilot-enabled cars had covered 130 million miles without a fatality, compared to a national average of one fatality every 94 million miles. Musk says it would be "morally reprehensible" to delay its rollout.

Tesla's Cars Have Driven 140M Miles on Autopilot. Here's How SEP --- Wired, 17 Aug 2016

Clicker: what is the problem with this statement?

SELF-DRIVING CARS

[Tesla] said Autopilot-enabled cars had covered 130 million miles without a fatality, compared to a national average of one fatality every 94 million miles. Musk says it would be "morally reprehensible" to delay its rollout.

Tesla's Cars Have Driven 140M Miles on Autopilot. Here's How SEP --- Wired, 17 Aug 2016

A RAND Corporation report concluded that fatalities and injuries are so rare that it would require an automated car to drive as many as hundreds of billions of miles before its performance could be fairly compared with statistics from the much larger population of human drivers.

https://www.technologyreview.com/s/601849/teslas-dubious-claims-about-autopilots-safety-record/

SERVICE UP-TIME

A fictitious school bus status update website claims 99.9% uptime.

Is this good?

SERVICE UP-TIME

A fictitious school bus status update website claims 99.9% uptime.

Is this good?

What if in the morning hours (5am - 8am) of a big snowstorm day, the website is down due to too much traffic.

With three such snowstorms a year, the website is down 9 hours out of a total of 365×24 hours per year.

9/8760 is roughly 0.1%. But the website is down when you most need it to be up!

P-VALUE

A New Study shows: A Glass Of Red Wine Is The Equivalent To



A new study shows: Searet to winning a Nobel prize? Eat



Scientists find the secret of longer life for men

[Daily Mail UK, 09/12]



Scientists find the secret of longer life for men (The bad news: castration is the key) [Daily Mail UK, 09/12]





Data Dredging



STATISTICAL TEST

Beer Consumption Increases Human Attractiveness to Malaria Mosquitoes

Beer (25):

27 20 21 26 27 31 24 21 20 19 23 24 28 19 24 29 18 20 17 31 20 25 28 21 27

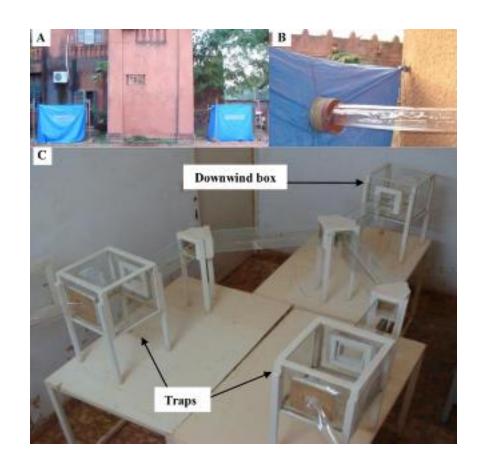
Mean: 23.6

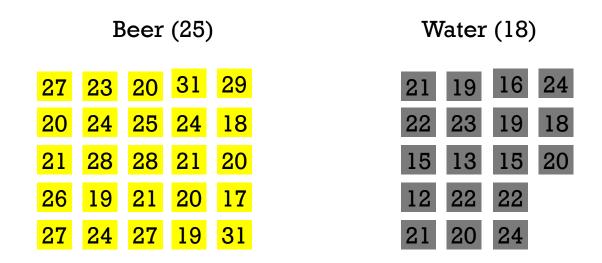
Water (18):

21 22 15 12 21 16 19 15 22 24 19 23 13 22 20 24 18 20

Mean: 19.2

Is a difference of 4.4 significant?

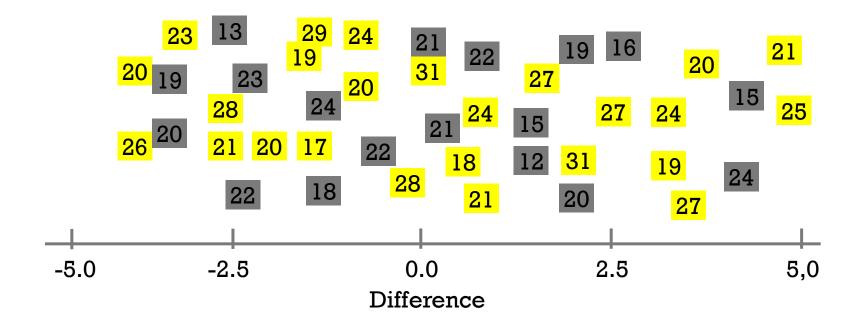




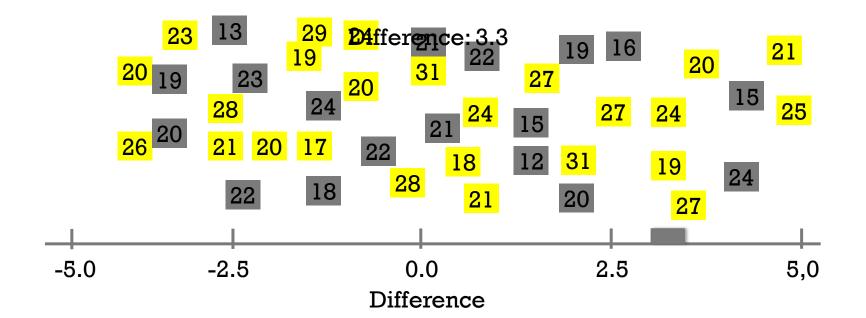
Difference: 4.4

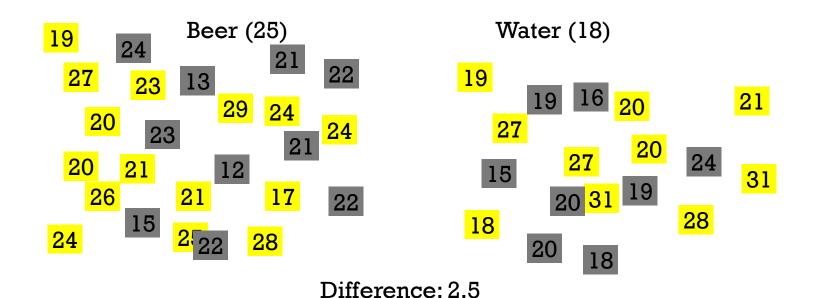


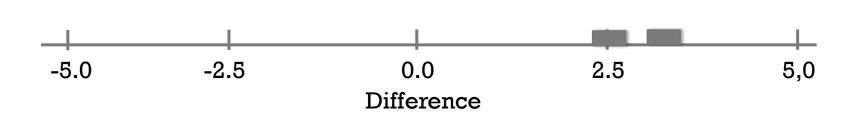
Beer (25) Water (18)

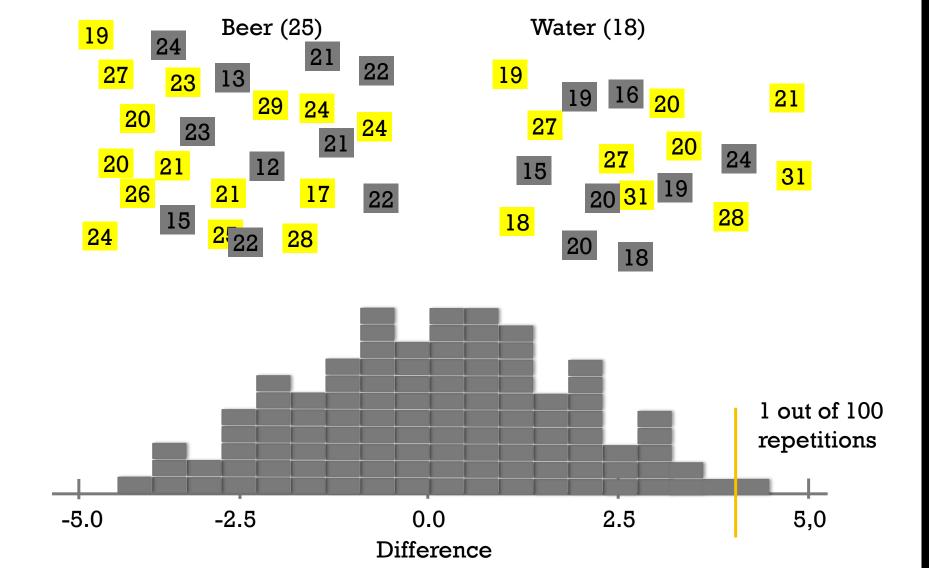


Beer (25) Water (18)

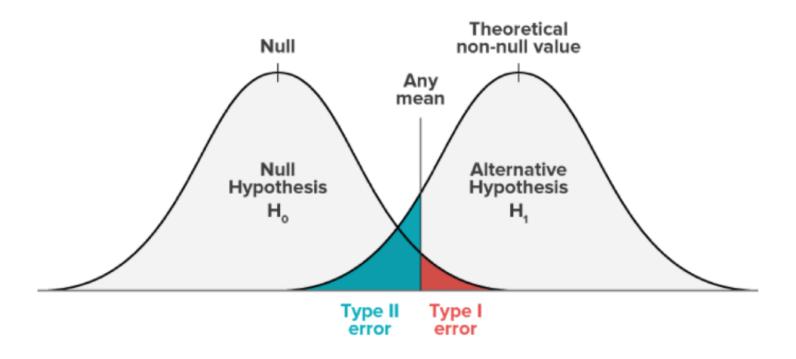








TYPE I VS TYPE II ERROR



The p value (Type I error) is the probability to obtain an effect equal to or more extreme than the one observed presuming the null hypothesis of no effect is true

P-VALUE HAS PROBLEMS!

BASIC AND APPLIED SOCIAL PSYCHOLOGY, 37:1-2, 2015

Copyright © Taylor & Francis Group, LLC ISSN: 0197-3533 print/1532-4834 online DOI: 10.1080/01973533.2015.1012991



Editorial

David Trafimow and Michael Marks

New Mexico State University

The Basic and Applied Social Psychology (BASP) 2014 Editorial emphasized that the null hypothesis significance testing procedure (NHSTP) is invalid, and thus authors would be not required to perform it (Trafimow, 2014). However, to allow authors a grace period, the Editorial stopped short of actually banning the NHSTP. The purpose of the present Editorial is to announce that the grace period is over. From now on, BASP is banning the NHSTP.

With the banning of the NHSTP from BASP, what are the implications for authors? The following are anticipated questions and their corresponding answers.

Question 1. Will manuscripts with p-values be desk rejected automatically?

Answer to Question 1. No. If manuscripts pass the

a strong case for rejecting it, confidence intervals do not provide a strong case for concluding that the population parameter of interest is likely to be within the stated interval. Therefore, confidence intervals also are banned from BASP.

Bayesian procedures are more interesting. The usual problem with Bayesian procedures is that they depend on some sort of Laplacian assumption to generate numbers where none exist. The Laplacian assumption is that when in a state of ignorance, the researcher should assign an equal probability to each possibility. The problems are well documented (Chihara, 1994; Fisher, 1973; Glymour, 1980; Popper, 1983; Suppes, 1994; Trafimow, 2003, 2005, 2006). However, there have been Bayesian proposals that at least somewhat circumvent

FICTIOUS EXAMPLE: BRAIN CANCER

Hypothesis: Brain cancer causes a headache

Data shows p<0.01 (considered very significant)

FICTIOUS EXAMPLE: BRAIN CANCER

Hypothesis: Brain cancer causes a headache

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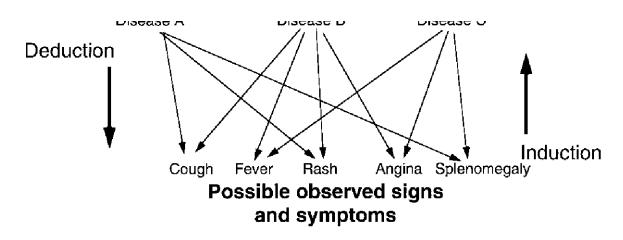
If you have a headache, how likely is it that you have brain cancer?

FICTIOUS EXAMPLE: BRAIN CANCER

Hypothesis: Brain cancer causes a headache

Data shows p<0.01 (considered very significant)

If you have a headache, how likely is it that you have brain cancer?



Statistical Inference

CLICKER: WHAT IS THE INTERPRETATION OF P < 0.05 HTTPS://CLICKER.MIT.EDU/6.S079/

- A) The chances are greater than 1 in 20 that a difference would be found if the study were repeated.
- B) The probability is less than 1 in 20 that a difference this large could occur by chance alone.
- C) The probability is greater than 1 in 20 that a difference this large could occur by chance alone.
- D) The chance is 95% that the study is correct
- E) None of the above

MISCONCEPTION 1

"In my experience teaching many academic physicians, when physicians are presented with a single-sentence summary of a study that produced a surprising result with P = 0.05, the overwhelming majority will confidently state that there is a 95% or greater chance that the null hypothesis is incorrect.

What is wrong with this?

MISCONCEPTION 1

"In my experience teaching many academic physicians, when physicians are presented with a single-sentence summary of a study that produced a surprising result with P=0.05, the overwhelming majority will confidently state that there is a 95% or greater chance that the null hypothesis is incorrect.

This is an understand- able but categorically wrong interpretation because the *P* value is calculated on the assumption that the null hypothesis is true. It cannot, therefore, be a direct measure of the probability that the null hypothesis is false. This logical error reinforces the mistaken notion that the data alone can tell us the probability that a hypothesis is true. "

"If P=.05, the null hypothesis has only a 5% chance of being true"

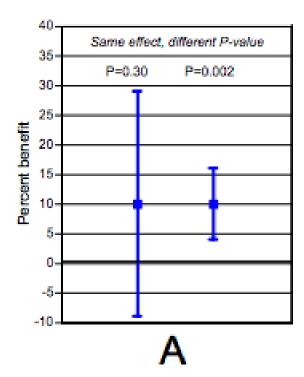
Let us suppose we flip a penny four times and observe four heads, two-sided P = .125. This does not mean that the probability of the coin being fair is only 12.5%.

A non significant difference (eg, P .05) means there is no difference between groups.

- A non significant difference only means the null effect is statistically consistent with the observation
- It does not make the null effect most likely
- In fact, the observed effect best explains the effect regardless the significance.

A statistically significant finding is (clinical) important

The P value carries no information about the magnitude of an effect, which is captured by the effect estimate and confidence interval.



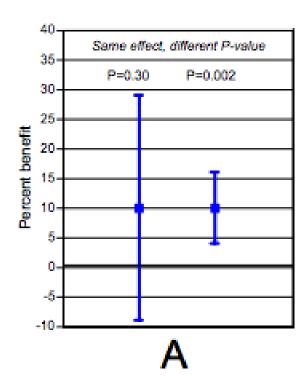
"Studies with P values on opposite sides of .05 are conflicting"

H₀:Drug T has no effect

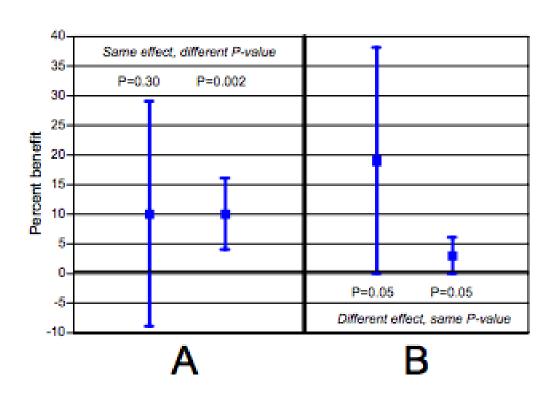
H₁:Drug T has a positive effect

Study I: P=0.3

Study II: P=0.002



Studies with the same P value provide the same evidence against the null hypothesis



P-VALUE HAS PROBLEMS!

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Editorial

David Trafimow and Michael Marks

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The Basic and Applied Social Psychology (BASP) 2014 Editorial emphasized that the null hypothesis significance testing procedure (NHSTP) is invalid, and thus authors would be not required to perform it (Trafimow, 2014). However, to allow authors a grace period, the Editorial stopped short of actually banning the NHSTP. The purpose of the present Editorial is to announce that the grace period is over. From now on, BASP is banning the NHSTP.

With the banning of the NHSTP from BASP, what are the implications for authors? The following are anticipated questions and their corresponding answers.

Question 1. Will manuscripts with p-values be desk rejected automatically?

Answer to Question 1. No. If manuscripts pass the

a strong case for rejecting it, confidence intervals do not provide a strong case for concluding that the population parameter of interest is likely to be within the stated interval. Therefore, confidence intervals also are banned from BASP.

Bayesian procedures are more interesting. The usual problem with Bayesian procedures is that they depend on some sort of Laplacian assumption to generate numbers where none exist. The Laplacian assumption is that when in a state of ignorance, the researcher should assign an equal probability to each possibility. The problems are well documented (Chihara, 1994; Fisher, 1973; Glymour, 1980; Popper, 1983; Suppes, 1994; Trafimow, 2003, 2005, 2006). However, there have been Bayesian proposals that at least somewhat circumvent

P-HACKING (ALSO DATA DREDGING, DATA FISHING, DATA SNOOPING, DATA BUTCHERY)

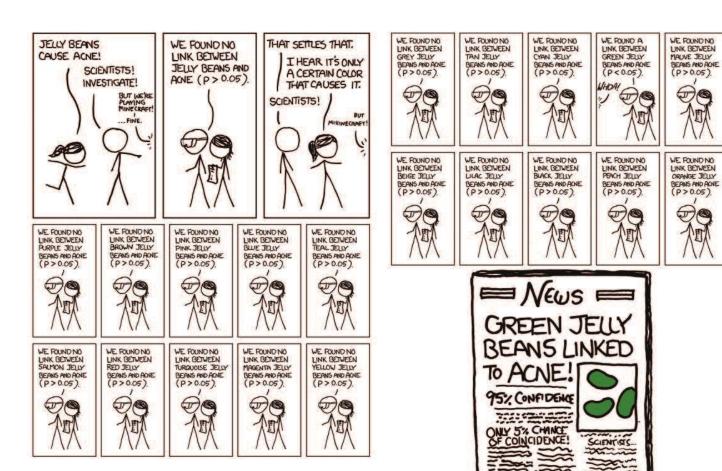


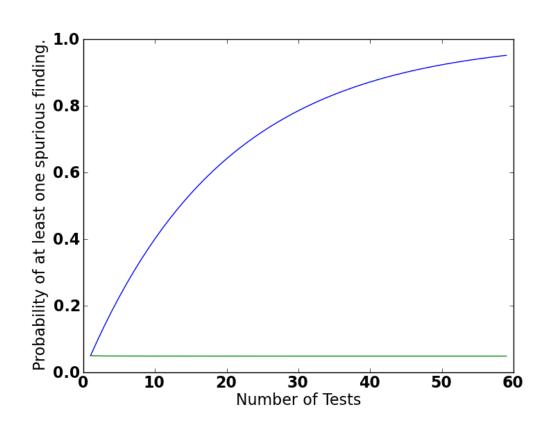
Figure 1. There is no overall effect of jelly beans on acne. Bummer. How about subgroups? Often subgroups are explored without alerting the reader to the number of questions at issue. Courtesy xkcd, http://xkcd.com/882/

P(detecting an effect when there is none) = α = 0.05

P(detecting an effect when it exists) = $1 - \alpha$

P(detecting an effect when it exists on every experiment) = $(1 - \alpha)^k$

P(detecting an effect when there is none on at least one experiment) = $1 - (1 - \alpha)^k$

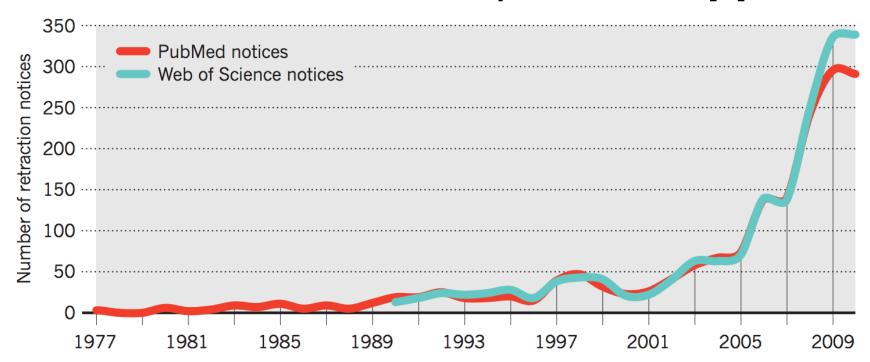


$$\alpha = 0.05$$

"Familywise Error Rate"

MISTAKES AND FRAUD

- 2001 2011: 10X increase in retractions
 - only 1.44X increase in papers



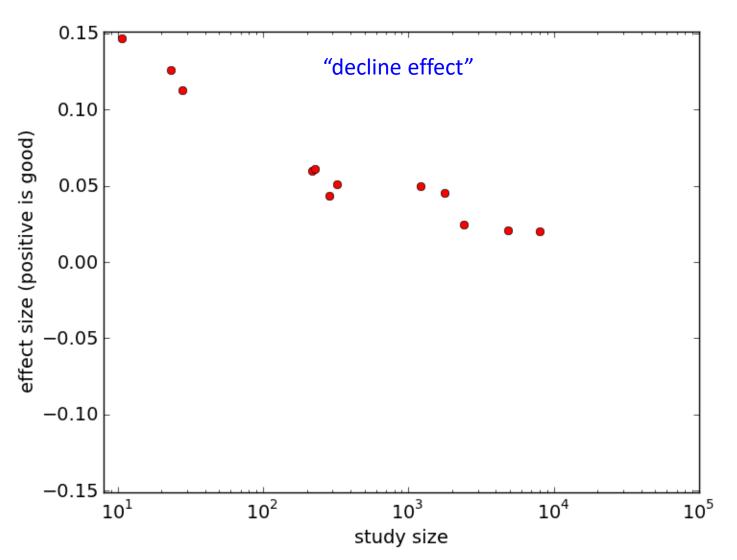
Richard Van Noorden, 2011, Nature 478

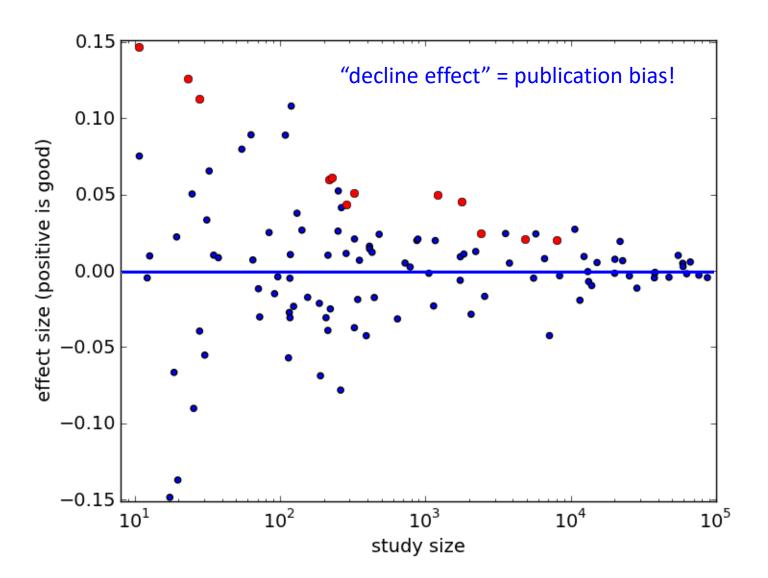
The Rise of the Retractions

http://www.nature.com/news/2011/111005/pdf/478026a.p

85

PUBLICATION BIAS





FAMILY-WISE ERROR RATE CORRECTIONS

Bonferroni Correction

Just divide by the number of hypotheses

Šidák Correction

Asserts independence

$$\alpha_c = \frac{\alpha}{k}$$

$$\alpha = 1 - (1 - \alpha_c)^k$$

$$\alpha_c = 1 - (1 - \alpha)^{\frac{1}{k}}$$



MANY ANALYSTS, ONE DATA SET

Variations in Analytic Choices Affect Results

Abstract: SEP

"Twenty-nine teams involving 61 analysts used the same data set to address the same research question: whether soccer referees are more likely to give red cards to dark-skin-toned players than to light-skin-toned players. Analytic approaches varied widely across the teams, and the estimated effect sizes ranged from 0.89 to 2.93 (Mdn = 1.31) in odds-ratio units. Twenty teams (69%) found a statistically significant positive effect, and 9 teams (31%) did not observe a significant relationship. Overall, the 29 different analyses used 21 unique combinations of covariates. Neither analysts' prior beliefs about the effect of interest nor their level of expertise readily explained the variation in the outcomes of the analyses. Crowdsourcing data analysis, a strategy in which numerous research teams are recruited to simultaneously investigate the same research question, makes transparent how defensible, yet subjective, analytic choices influence research results."

CLOSING THOUGHTS

"It is easy to lie with statistics, but it is easier to lie without them."

attributed to Frederick Mosteller (1916-2006)

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